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## Study Guide

## Solving Systems of Linear Inequalities

To solve a system of linear inequalities, you must find the ordered pairs that satisfy all inequalities. One way to do this is to graph the inequalities on the same coordinate plane. The intersection of the graphs contains points with ordered pairs in the solution set. If the graphs of the inequalities do not intersect, then the system has no solution.

## Example 1 Solve the system of inequalities $-x+2 y \leq 2$ by graphing. <br> $x \leq 4$

The shaded region represents the solution to the system of inequalities.

A system of more than two linear inequalities can have a solution that is a bounded set of points called a polygonal convex set.


Example 2 Solve the system of inequalities $x \geq 0$ by graphing and name the $\quad y \geq 0$ coordinates of the vertices of $\quad 5 x+8 y \leq 40$ the polygonal convex set.
The region shows points that satisfy all three inequalities. The region is a triangle whose vertices are the points at $(0,0),(0,5)$, and $(8,0)$.


Example 3 Find the maximum and minimum values of $f(x, y)=x+2 y+1$ for the polygonal convex set determined by the following inequalities. $x \geq 0 \quad y \geq 0 \quad 2 x+y \leq 4 \quad x+y \leq 3$
First, graph the inequalities and find the coordinates of the vertices of the resulting polygon.


The coordinates of the vertices are ( 0,0 ), $(2,0),(1,2)$, and ( 0,3 ).

Then, evaluate the function $f(x, y)=x+2 y+1$ at each vertex.

$$
\begin{array}{ll}
f(0,0)=0+2(0)+1=1 & f(1,2)=1+2(2)+1=6 \\
f(2,0)=2+2(0)+1=3 & f(0,3)=0+2(3)+1=7
\end{array}
$$

Thus, the maximum value of the function is 7 , and the minimum value is 1 .
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## Practice

## Solving Systems of Linear Inequalities

Solve each system of inequalities by graphing.

1. $-4 x+7 y \geq-21 ; 3 x+7 y \leq 28$

2. $x \leq 3 ; y \leq 5 ; x+y \geq 1$


Solve each system of inequalities by graphing. Name the coordinates of the vertices of the polygonal convex set.
3. $x \geq 0 ; y \geq 0 ; y \geq x-4 ; 7 x+6 y \leq 54$

4. $x \geq 0 ; y+2 \geq 0 ; 5 x+6 y \leq 18$


Find the maximum and minimum values of each function for the polygonal convex set determined by the given system of inequalities.
$\begin{array}{ll}\text { 5. } 3 x-2 y \geq 0 & y \geq 0 \\ 3 x+2 y \leq 24 & f(x, y)=7 y-3 x\end{array}$

6. $y \leq-x+8 \quad 4 x-3 y \geq-3$ $x+8 y \geq 8 \quad f(x, y)=4 x-5 y$

7. Business Henry Jackson, a recent college graduate, plans to start his own business manufacturing bicycle tires. Henry knows that his start-up costs are going to be $\$ 3000$ and that each tire will cost him at least $\$ 2$ to manufacture. In order to remain competitive, Henry cannot charge more than $\$ 5$ per tire. Draw a graph to show when Henry will make a profit.

